

# 1 Spatio-Temporal Entropy Analysis Of The Magnetic 2 Field To Help Magnetic Cloud Characterization

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**Abstract.**

The aim of this work is to create a methodology to characterize the dynamics of magnetic clouds (MCs) from signals measured by satellites in the interplanetary medium. We have tested Spatio-Temporal Entropy (STE) technique to study 41 MCs identified by other authors, where the plasma sheath region has been identified. The STE was implemented in Visual Recurrence Analysis (VRA) software to quantify the order in the recurrence plot. Some tests using synthetic time series were performed to validate the method. In particular, we worked with IMF components  $B_x$ ,  $B_y$ ,  $B_z$  of 16 s. Time windows from March 1998 to December 2003 for some MCs were selected. We found higher STE values in the sheaths and zero STE values in some of the three components in most of the MCs (30 among 41 events). The trend is the principal cause of the lower STE values in the MCs. Also, MCs have mag-

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16 netic field more structured than sheath and quiet solar wind. We have done  
17 a test considering the magnetic components of a cylindrically symmetric force-  
18 free constructed analytically, with the result of zero STE value. It agrees with  
19 the physical assumption of finding zero STE values when studying experi-  
20 mental data in MC periods. The new feature just examined here adds to the  
21 usual features, as described in Burlaga et al. [1981], for the characterization  
22 of MCs. The STE calculation can be an auxiliary objective tool to identify  
23 flux-ropes associated with MCs, mainly during events with no available plasma  
24 data but only with IMF.

## 1. Introduction

25 The term magnetic cloud (MC) has been used to characterize an Interplanetary Coronal  
26 Mass Ejection (ICME) that presents a specific configuration, in which the magnetic field  
27 strength is [higher than average IMF](#), the magnetic field direction rotates smoothly through  
28 a large angle, and the proton temperature is low [Burlaga et al., 1981; Klein and Burlaga,  
29 1982; Gosling, 1990]. Typically a flux-rope ejected from the Sun described the magnetic  
30 configuration of a MC. The MCs are observed in a clear way when the spacecraft crosses  
31 the magnetic field structure close by its center [Schwenn, 2006]. *In-situ* measurements are  
32 limited to the spacecraft trajectory crossing the incoming ICME. Therefore, one needs  
33 to rely on modeling evaluation in order to derive the global magnetic structure from  
34 available local measurements [Démoulin and Dasso, 2009]. [Due to MCs moving faster](#)  
35 [than the surrounding solar wind \(SW\), plasmas and magnetic field typically accumulate](#)  
36 [in front of it, creating a preceding disturbed sheath.](#)

37 In Ojeda et al. [2005], a study considering 20 MCs, 17 [non-MC ICMEs](#), and 20 time  
38 series of equivalent time duration of quiet SW was done. The IMF  $B_z$  and solar wind  $V_x$   
39 components in a time interval of 48 h before each MC were analyzed. Under MC con-  
40 ditions, a feature was identified that the component  $B_z$  of the IMF has the tendency to  
41 present lower spatio-temporal entropy (name given by Eugene Kononov's Visual Recur-  
42 rence Analysis (VRA) software, not to be confused with spatio-temporal entropy image  
43 (STEI) [Ma and Zhang, 2001]) values than the  $B_z$  in other cases, such as in [non-MC](#)  
44 [ICMEs](#) and during quiet SW. This behavior seems to be very interesting under a physical  
45 point of view. Thus in this work a more detailed study of the spatio-temporal entropy

46 (STE) in MCs is carried out. The analyses are expanded to study the three magnetic  
 47 components ( $B_x$ ,  $B_y$  and  $B_z$ ) using more complete dataset. The aim of this work is to  
 48 validate the STE calculation technique as an useful tool to identify features of the MCs.  
 49 A proposed approach to study the MCs by analyzing the time series of interplanetary  
 50 magnetic field (IMF) is presented.

51 The content is organized as follows. In Section 2, a review on the theoretical and obser-  
 52 vational aspects of the interplanetary MCs is presented. In Section 3, the dataset used is  
 53 described. In Section 4, a STE methodology for analyses is established. In Section 5, we  
 54 compare STE values for time series corresponding to the MCs and the sheaths identified  
 55 by Huttunen et al. [2005]. Finally, in Section 6 the conclusions are done. In Appendices,  
 56 information on the tool is presented. Appendix A, shows a review on the tool in the VRA  
 57 software. And Appendix B, the methods for calculating the entropy in the recurrence  
 58 plot.

## 2. Magnetic Clouds

59 The pioneer studies on plasma clouds emitted by the Sun were developed about  
 60 1950s [Morrison, 1954; Cocconi et al., 1958; Piddington, 1958]. However the definition  
 61 and the term of "magnetic cloud" were presented by the first time in the work of Burlaga  
 62 et al. [1981]. Nowadays the specific signatures which have to be necessarily fulfilled are  
 63 the following: (1) smooth rotation in  $\vec{B}$  with low variance; (2) low proton temperature  
 64 and (3) low plasma  $\beta$ , which is the ratio of the plasma pressure,  $p = nk_B T$ , to the mag-  
 65 netic pressure,  $p_{mag} = B^2/2\mu_0$  where  $n$  is number density,  $K_B$  Boltzmann constant,  $T$   
 66 temperature,  $B$  magnetic field and  $\mu_0$  magnetic permeability of the free space.

67 Initial studies to analyze the three-dimensional configuration of the magnetic field of  
68 these [phenomenon have been](#) developed by Burlaga et al. [1981]. The minimum variance  
69 analysis (MVA) was used as a method to identify and describe planar magnetic field  
70 configuration associated with thin current sheets in the SW [Burlaga and Klein, 1980]  
71 and planetary magnetospheres [Lepping and Behannon, 1979]. Burlaga et al. [1981] used  
72 MVA to analyze the magnetic field configuration in a MC observed with 4 spacecraft:  
73 Voyager 1 and 2, IMP 8, and Helios 2. They concluded that MC could be represented  
74 as a magnetic cylinder whose axis lies close in the equatorial plane, marking an angle of  
75 nearly  $90^\circ$  with respect to the radial direction.

76 Considering a cylindrical geometry for MCs, the MVA [Sonnerup and Cahill, 1967] re-  
77 sulted an useful tool to calculate the direction of the cloud axis. Klein and Burlaga [1982]  
78 identified 45 events in the period between 1967 and 1978, where the latitude and longitude  
79 of the clouds axis were calculated. The results of Burlaga et al. [1981] also were consistent  
80 with other configurations. Ivanov and Harshiladze [1984] created a mathematical formula-  
81 tion using a cloud configuration as an oblate ellipsoidal. To understand how the magnetic  
82 field configuration evolves in the SW may be necessary for the correct interpretation of  
83 the field structure in MC [Burlaga and Behannon, 1982].

84 Goldstein [1983] considered a force-free configuration in the search for a stable topology  
85 of the MCs. Marubashi [1986] studied interplanetary magnetic field data from the Pio-  
86 neer Venus orbiter (PVO) between December 1978 to May 1984 in search of interplanetary  
87 magnetic flux ropes near the Venus orbit. As a result, twenty-six well defined flux ropes  
88 were found which have characteristics similar to those of flux ropes observed near Earth.  
89 In one case, where the Sun, Venus and Earth were closely aligned, an almost identical

90 structure was observed by the PVO and the Earth-orbiting spacecraft with a time delay  
91 of about 36 hours. This observation provides evidence that the structure of interplanetary  
92 magnetic flux ropes are maintained during propagation at least from 0.72 AU (Astronom-  
93 ical Unit (AU): The average distance from the Earth to the Sun. One AU = 93 million  
94 miles or 149.6 million km) to 1 AU. A simple solution for a cylindrically symmetric  
95 force-free field with constant alpha was studied by Lundquist [1950], and mentioned also  
96 in Lundquist [1951]. Burlaga [1988] studied the above solution with constant alpha to  
97 describe the types of signatures observed in the SW at 1 AU when MCs move past a  
98 spacecraft.

99 In order to find plasma beta values significantly lower than one to identify MCs, space-  
100 craft measurements of magnetic field and plasma are required. Sometimes the temperature  
101 and density data on spacecraft have many gaps during periods in which the plasma in-  
102 struments are saturated as a result of intense particle fluxes (for example, Bastille Day in  
103 the ACE spacecraft). If this condition occurs, it makes impossible to calculate the plasma  
104 beta, but it is still possible to detect the MC using magnetometers data [e.g., Huttunen  
105 et al., 2005; Nieves-Chinchilla et al., 2005]. Here is the contribution we intend to do with  
106 this work, showing an approach that could help to identify MCs, and it is proposed as  
107 basis for an auxiliary analysis tool.

108 The main contributions related to the identification of MCs are summarized in Table 1.  
109 It was adapted from Huttunen et al. [2005] and updated by us. We show in each column  
110 of this table, the paper, the period of the investigation, the examination period ( $T_t$ ),  
111 the spacecraft used (Spacf), and the quantities number of MCs identified. Bothmer and  
112 Rust [1997]; Bothmer and Schwenn [1998]; Huttunen et al. [2005] identified MCs based

113 on the MVA method; Mulligan et al. [1998] identified and classified MCs using the visual  
 114 inspection of the data; Lynch et al. [2003] and Wu et al. [2003, /WIND list] used the least-  
 115 square fitting routine by Lepping et al. [1990]; while Nieves-Chinchilla et al. [2005] studied  
 116 all the MCs observed during the time interval 2000 – 2003 using the elliptical cross-section  
 117 model [Hidalgo, 2003, 2005], where a distortion and expansion of the cross-section of the  
 118 cloud is included from first principles.

119 From 1997 – 2003 in solar cycle 23, SW data were investigated by Huttunen et al.  
 120 [2005] using the MVA method [Sonnerup and Cahill, 1967; Bothmer and Schwenn, 1998]  
 121 to determine if they have flux-rope structures. They identified 73 MCs observed by the  
 122 ACE and WIND spacecraft. In principle the axis of a MC can have any orientation  
 123 with respect to the ecliptic plane [Bothmer and Schwenn, 1994, 1998], identified by the  
 124 azimuthal direction in the ecliptic, called  $\phi_C$ , and the inclination relative to the ecliptic,  
 125 called  $\theta_C$ . With the MVA, the angles above can be calculated [Bothmer and Schwenn,  
 126 1998]. In order to classify MCs [Huttunen et al., 2005, and references therein], eight flux  
 127 rope categories are often used, clustered as: Bipolar MCs (low inclination, and flux rope-  
 128 type: SWN, SEN, NES, NWS),  $\theta_C \leq 45^\circ$  and Unipolar MCs (high inclination, and flux  
 129 rope-type: WNE, ESW, ENW, WSE),  $\theta_C > 45^\circ$ , where the meanings are S for south, N  
 130 North, W west and E east.

131 Huttunen and collaborators have also included seven cloud candidate events for which  
 132 either the fitting with MVA was not successful (e.g. the eigenvalue ratio  $< 2$  or the  
 133 directional change less than  $30^\circ$ ) or there were large values of beta throughout the event.  
 134 In their study, [the criterion to identify a MC was based on the smoothness of the rotation](#)  
 135 [in the magnetic field direction confined to one plane. Additionally they required that a](#)



136 MC must have the average values of the plasma beta less than 0.5, the maximum value  
137 of the magnetic field at least 8 nT, and the duration at least 6 h. The last two criteria  
138 have been created with the objective of exclude “small and weak MCs”. All selected  
139 events were investigated by analyzing 1 h magnetic field data with the minimum variance  
140 analysis (MVA), where MCs are identified from the smooth rotation of the magnetic field  
141 vector in the plane of the maximum variance [Klein and Burlaga, 1982]. For MCs with  
142 durations of 12 h or less Huttunen et al. [2005] performed MVA using 5-min (WIND) or  
143 4-min (ACE) averaged data.

### 3. IMF Dataset

144 The IMF dataset used in this work are measurements obtained by the ACE satellite.  
145 The ACE spacecraft is in orbit around  $L1$  from 1997 [Smith et al., 1998]. Where the  
146 Lagrangean point  $L1$  is a gravitational equilibrium point between the Sun and Earth at  
147 about 1.5 million km from Earth and 148.5 million km from the Sun. On board of ACE a  
148 total of ten instruments, was launched toward  $L1$  [McComas et al., 1998], but in this work  
149 only the Magnetic Field Experiment (MAG) is used. The MAG on board ACE consists  
150 of twin vector fluxgate magnetometers to measure the IMF [Smith et al., 1998]. The data  
151 (<http://www.srl.caltech.edu/ACE/ASC/level2/index.html>) contains time averages of  
152 the magnetic field over time periods 1 s, 16 s, 4 min, hourly, daily and 27 days (1 Bartels  
153 rotation). In this work, IMF components ( $B_x$ ,  $B_y$ ,  $B_z$ ) with time resolution of 16 s in  
154 GSM coordinate systems are used.

155 We only work with 41 of 73 MCs identified by Huttunen et al. [2005] from March  
156 1998 to December 2003: where the MCs were preceded by the plasma sheaths. We are  
157 interested in comparing these two regions when it have been well identified. The 41 events

158 in chronological order are shown in Table 2 and 3. The columns from the left to the right  
159 give: a numeration of the events, year, shock time (UT), MC start time (UT) and MC  
160 end time (UT) respectively.

#### 4. Methodology Using STE Analysis

161 Based on the description of MCs, a proper statistical tool can be used to identify their  
162 typical features. The STE analysis was chosen to establish a methodology. The STE  
163 analysis consists of a tool that compares the distribution of distances between all pairs  
164 of vectors in the reconstructed state space with that of distances between different orbits  
165 evolving in time. In this context, the terms “state space” and “orbits” are concepts of  
166 the theory of chaotic dynamical systems. State space reconstruction is the first step in  
167 non-linear time series analysis of data from chaotic systems including estimation of invari-  
168 ants and prediction. Dynamical regimes, such as a resting state or periodic oscillation,  
169 correspond to geometric objects, such as a point or a closed curve, in the phase space.  
170 Evolution of a dynamical system corresponds to a trajectory (or an orbit) in the phase  
171 space. Different initial states result in different trajectories. In the recurrence plot (RP) a  
172 one-dimensional time series from a data file is expanded into a higher-dimensional space,  
173 in which the dynamic of the underlying generator takes place. The concept of state space  
174 and orbit are also valid in the RP and in the subsequent calculation of the STE. The STE  
175 results identify in a certain objective way the characteristics of a physical process present  
176 in a time measurement dataset.

177 The VRA software provides resources to investigate this promising approach immedi-  
178 ately. The recurrence plot has been used. For more details, the information on it is  
179 presented in Appendix A (recurrence plot) and Appendix B (entropy).

180 In this section, the purpose is to show the variation of STE values after processing  
181 carried out in some synthetic time series, file included in VRA software. The methodology  
182 to study synthetic time series will be implemented, with the purpose to be applied to  
183 analyse IMF dataset.

#### 4.1. STE Variations Versus Trend Angle

184 From an intuitive point of view, a time series is said to be stationary if there has not  
185 trend and no systematic change in variance and if strictly periodic variations have been  
186 removed [Chartfield, 2003]. Trend estimation is a statistical technique that could be aid in  
187 the interpretation of data [Chartfield, 2003]. When a time series related to measurements  
188 of a process are treated, trend estimation can be used to make and justify statements  
189 about tendencies in the data. Given a set of data and the desire to produce some kind  
190 of function fitted through of those data the simplest function to fit is a straight line  
191 (using least-squares fit). If there is no global trend in time series the angle (“trend angle”)  
192 between the straight line and the positive  $x$  axis must be zero.

193 We have calculated the STE value for each temporal series with embedding dimension  
194 and time delay equal to 1 respectively. It may be noticed that STE value changes for dif-  
195 ferent embedding parameters. For example, for Lorenz attractor (Lorenz data file included  
196 in VRA), STE is near its minimum when the correct embedding is used (dimension = 3,  
197 time delay = 16 to this particular data file). This and other results suggest that STE can  
198 be used to determine the optimal embedding parameters, that is not the aim in this work.  
199 We selected the same embedding and time delay, equal to one, to maintain equivalence  
200 in the calculation of STE among all series in order to compare the results. Because our

201 hypothesis is that this tool (STE) could be useful in a computational implementation to  
202 characterize MCs or used as a new property of them.

203 With the VRA software a group of synthetic time series were included. It were included  
204 a variety of time series with different properties, i.e. periodic, random, with noises and  
205 chaos respectively. A dataset of time series, Lorenz, Sine and White Noise, are used as  
206 test cases to validate the STE calculation.

207 Figure 1 shows a time series plot of Lorenz data file included in VRA software. We gave  
208 trends to the series through angular rotations about the origin. Time series have 3500  
209 data records and it were rotated about the origin, angles of  $0 \text{ rad}$ ,  $-0.01 \text{ rad}$ ,  $0.01 \text{ rad}$   
210 and  $0.0175 \text{ rad}$  respectively. The STE values have been calculated for each time series  
211 and the results are shown in Table 4, row 2. In Table 4 in the five columns are shown:  
212 time series data file included in VRA version 4.7; these time series are rotated about the  
213 origin with [the previous angles](#); and it is calculated the STE values of each time series.

214 We follow the same idea, to cause a trend in time series for another cases, Sine and  
215 White Noise data file also included in VRA software. The results have been included in  
216 rows 3 and 4 in Table 4. In periodic time series (sine data file) the STE value is always zero  
217 independently of increasing trend. In the other two cases, if time series trend increases  
218 then the STE values decreases (see row 2 and 4 in Table 4). We are doing those kinds of  
219 tests because we know that inside MCs the trend of IMF components increase; and we  
220 are interested in knowing how it could affect STE values.

221 To go on with the above idea is good to know that: the time series of the first difference  
222 is often enough to convert series with a trend into a stationary time series. The first-  
223 order differences of time series values  $x_1, x_2, x_3, \dots, x_N$  are given by a new series

224  $y_1, y_2, \dots, y_{N-1}$ , where  $y_{N-1} = x_N - x_{N-1}$ . The operation  $y_t = x_t - x_{t-1} = \nabla x_t$  is called  
225 the first difference and  $\nabla$  is the difference operator [Chartfield, 2003].

226 Our interest is to study variations in the STE values when first-order differences are  
227 applied on stationary time series. In time series studied previously (Lorenz, Sine and  
228 White Noise), new time series from the first-order differences have been constructed.  
229 After that, we calculated STE values of each time series and the results were compared  
230 with the original series (non differentiated or untransformed) shown in Table 5. The  
231 STE values are similar in both of them, *i.e.*, for transformed (first-order differences) and  
232 untransformed time series. Thus, if the time series has non trend then the non-linear  
233 delicate structures are not destroyed.

234 The STE value is low and may tend to zero in any time series with trend. [If there is a](#)  
235 [trend in the time series, it could be removed by differencing the original time series before](#)  
236 [calculating the STE. However, taking the first differences may interfere with the delicate](#)  
237 [nonlinear structure in the time series \(if there is any\).](#) Thus STE values are calculated  
238 on the untransformed series and then in the transformed series, where the first-order  
239 differences is applied. This is done on a trial basis after calculating STE values of the  
240 original series.

## 4.2. Variations Of STE Values Given By Time Series Size

241 The calculation of the STE with the VRA software, version 4.7, can not be made in  
242 time series with size larger than  $\sim 5000$  points because the STE has a rapid decrease  
243 to zero. It seems to be a limitation of the software by some reason not explained in its  
244 tutorial. To exemplify the previous statement, synthetic series have been created using  
245 a [pseudorandom number generator \(PRNG\)](#) producing values in the range 0 to 1. In

246 Figure 2 (top panel), an example with 3000 points is shown. In this time series a STE  
247 value of 86% was calculated. The Figure 2 (bottom panel) shows the plot of STE values  
248 versus  $\text{length}(X(t))$  of 18 time series constructed as shown in the top panel. The STE  
249 values decrease in time series with a length larger than  $\sim 4000$  points. When using the  
250 VRA software someone must take into account this identified limitation in the extension  
251 (length) of the data under analysis.

### 4.3. Scheme To Study STE Values In IMF Components

252 Figure 3 show the scheme that will be used to characterize MCs. From the 73 that have  
253 been identified by Huttunen et al. [2005] from March 1998 to December 2003 are selected  
254 41 of them, the cases where the plasma sheath also is identified. For both regions, time  
255 series of IMF components with time resolution of 16 s, in GSM coordinates system, are  
256 selected. Using VRA software the data without transformations are processed. Also the  
257 same data before using the software are transformed. The aim of the transformations  
258 is to eliminate the trend and noises respectively. The trends are eliminated with two  
259 techniques, e.g. doing first order differences at time series and a rotation about the origin,  
260 in the beginning of this section both techniques were explained. To filter the white noise  
261 a Gaussian filter can be used, e.g. Mendes et al. [2006]. Inside the VRA software the RPs  
262 are generated and the STE values are calculated.

263 Using a simple solution for a cylindrically symmetric force-free field with constant alpha  
264 [Burlaga, 1988], time series were constructed. To a physical evaluation, the STE values  
265 are calculated. Finally, with the results, the MCs are characterized.

## 5. Results And Discussion

266 The STE values for the 41 MC events are shown in Figure 4. At the top, the STE  
 267 values calculated from the three IMF components  $B_x$ ,  $B_y$  and  $B_z$ , plotted respectively as  
 268 “o”, “+” and “x”, corresponding to MCs. At the bottom, the same of above but for  
 269 the sheath regions. The STE values of the 246 time series ( $3 * (41MCs + 41Shts) = 246$ ),  
 270 were plotted in chronological order as appeared in Table 2 column 1. Some MCs do not  
 271 have STE values close to zero in the three components simultaneously. Then, it is possible  
 272 to find components with perfect structuredness (low STE) and absence of structure (high  
 273 STE) in the same MC.

274 If STE values between the same components for the plasma sheath and the MC regions  
 275 are compared (e.g.  $B_x$ -sheath ( $STE = 56\%$ ) with  $B_x$ -cloud ( $STE = 0\%$ ) in the event  
 276 number 1), then in 5/41 (3/41) of the cases, in the  $B_x$  ( $B_y$ ,  $B_z$ ) component(s), the STE  
 277 value in the MC is larger than at its plasma sheath region respectively. These are few  
 278 cases, and show a clear tendency to decrease the STE value within the MC region in all  
 279 IMF components. Someone can notice a clear tendency of the cloud events to present STE  
 280 with lowest values, close to zero, as was noticed for  $B_z$  in Ojeda et al. [2005] and extended  
 281 in this work, proposed as new feature adding to the usual features [Burlaga et al., 1981]  
 282 established to the MCs.

283 Other interesting result is that STE values are zero in 20/41, 21/41, 26/41 MCs to  
 284  $B_x$ ,  $B_y$ ,  $B_z$  components respectively. The three components has zero entropy ( $STE =$   
 285  $0\%$ ) at the same time in 17/41 MCs and 1/41 sheaths. The plasma sheath region with  
 286  $STE = 0\%$  corresponds to event number 06 at Table 2.

287 Figure 5 shows a histogram of STE derived from Figure 4 for the  $B_z$  component corre-  
 288 sponding to MCs (in black) and plasma sheaths (in grey) regions respectively. We have

37/41 or 90.2% of MCs with STE less than 40%. However, if we analyze the plasma sheath, then the result is exactly opposite, we found 37/41 or 90.2% of sheaths with STE larger than 40%. This shows the great difference between the two regions: the sheath is a turbulent region [Chian and Muñoz, 2011] where the plasma and magnetic field typically accumulate in ahead of the MC and cause fluctuations in the magnetic field. Thus, the time series could have more noise and therefore large STE values. In particular, the magnetic configuration of a MC could be described by a flux-rope with cylindrical geometry where the magnetic field has slow rotation along one day increasing the trend and decreasing the noise and therefore the STE values decrease. Low-entropy structures were found in the solar wind [e.g. Neugebauer et al., 2004], and physically we expected to find low entropy in the cloud. But the novel result shows that large amount of MCs with  $STE = 0\%$  has been found.

We did some tests with time series to explain the above results. First, if the Gaussian noise is removed from the signal and the STE calculated, the STE value tend to decrease in less than 5% from its initial value. Second, when a trend is removed of the time series through a rotation (with the angle of slope line of best fit) the STE varies, but still the three components had  $STE = 0\%$  at the same time in 17/41 MCs and 1/41 sheaths (see Figure 8, top panel). Third, by removing the trend through the first order difference in time series (see Figure 6). After that, there are still MCs with  $STE = 0\%$ .

In Figure 6 the study is the same as in Figure 4, but we have eliminated the trend through the first order difference in time series as mentioned in Section 4. In this case, most of calculating the STE values of all three components increased to  $\sim 90\%$  in the plasma sheaths. Figure 7 shows a histogram of STE values in  $B_z$  component of MCs



312 and sheaths derived from Figure 6. If we eliminate the trend in the time series, then the  
 313 STE value increase. Leaving now 11 of a total of 27 MCs (see Figure 5) with STE values  
 314 between 0% and 10%. Also the STE increases in the MC region, but there are still MCs  
 315 with zero STE value.

316 Due to a software limitation, presented earlier (Figure 2), we investigated the effect of  
 317 the length of the time series that have studied in Figure 4. Then, in Figure 8 (top panel),  
 318 a plot of STE versus length of  $B_z$  time series for all MCs are shown. The “o” and “+”  
 319 symbols correspond to the original and transformed (removing the Gaussian noise and  
 320 “trend” through a rotation about the origin) time series respectively. A vertical line was  
 321 drawn in the point with  $length(B_z) = 5500$  points. To the right of the vertical line, due  
 322 to a software limitation (this was discussed in the end of section 4) the STE value is zero.

323 In Figure 8 (bottom panel) the histogram of the original or untransformed time series  
 324 helps to identify overlapping points of MC that are shown in the top panel. Exist a total  
 325 number of 17/41 MCs with zero STE values to the right of the vertical line. These are  
 326 the events 1 – 4, 6 – 10, 13, 16, 27, 30, 33 – 35, 40 shown in Table 2. This is a problem  
 327 because the larger MCs are just the best structured. However, there still 9/41 MCs with  
 328 zero STE values to the left of the vertical line, these are the events 5, 12, 21, 23 – 25,  
 329 31, 32, 37 shown in Table 2. Event No. 38 has  $STE = 6\%$  and complete the total of 27  
 330 events with STE between 0 – 10% shown in the histogram at Figure 5.

331 In Figure 8 the STE values of the transformed time series (“+” symbol) increase and  
 332 are different from zero in the MC with less than 5500 points. The smooth increase of  
 333 trend occur in time series of IMF in a MC and is caused by the travel of an organized  
 334 structure in form of flux-rope, crossing the spacecraft. The trend grows smoothly for the

335 IMF in a MC with length less than 5500 and are the main causes of lower STE values.  
336 Since the STE results of this tool can be affected by the trend, this tool could be useful in  
337 computational applications to identify MC regions, but failed to identify the boundaries  
338 of them.

339 In Figure 9 the study is the same as in Figure 8, but for the plasma sheaths regions.  
340 The length of the sheaths have less points than the MCs, only one sheath had more than  
341 5500 points, the event number 6 shown in Table 2. Both histograms at the Figures 8 and  
342 9 are constructed only to help in the visualization of the distribution of lengths at the top  
343 panels of it. The main result is that the STE values in the sheaths, of the transformed  
344 time series (“+” symbol), are approximately the same as the original (“o” symbol) time  
345 series. We conclude that the trend in the plasma sheath is less important and STE have  
346 large values.

347 To study the true STE values of the MC with more than 5500 points and overcome the  
348 software limitation, we have two options: (1) select data with other temporal resolution  
349 (i.e., it to become poor the data information); or (2) select a MC sample with less than  
350 5500 points. We performed option 2, taking the intervals from the positions 500 (to avoid  
351 effects caused by the identification of the boundaries) to 4500 in IMF  $B_z$ . Thus, the length  
352 of the time series reconstructed is 4001 data points. These 17/41 cases represented by  
353 “×” symbol are shown in Figure 10 (top panel); the “o” symbol represent non-transform  
354 MCs similar to 8. In the right hand of the vertical line, the MCs sample (“×” symbol  
355 and 4001 data points) are plotted in the position with same length of non-transform MCs  
356 (“o”). Only 1/17 case remains with zero STE and a total of 4/17 events remains with  
357 STE less than 11%. To make a better comparison, the histogram in the bottom panel at

358 Figure 10 was built. We have 33/41 or 80.5% of MCs with STE less than 40%. Still a  
359 good percentage (80.5%) that enables us to keep the findings of low STE in MCs.

360 A physical interpretation can be established as following. It was observed during the  
361 data processing that entropy values less than 40% could appear only in one or two of the  
362 three components of the MCs. This has a physical explanation: magnetic field axis of  
363 a magnetic flux-rope in a MC could have different inclinations. Then, the trend of IMF  
364 components is larger in a plane or one direction. It is advisable to work in a reference  
365 frame found by a MVA analysis. So far, we have been seeking the causes of the large  
366 amount of MCs with  $STE = 0\%$ . During a MC, the magnetic field strength is higher  
367 than the average, the magnetic field direction rotates smoothly through a large angle,  
368 then the periods with MCs present more trend in the magnetic behavior than the periods  
369 of sheaths or quiet SW. The trend is the principal cause of the lower STE values in MC.

370 To demonstrate quantitatively all results that have been shown up here, a simple  
371 solution for a cylindrically symmetric force-free field with constant alpha [Lundquist,  
372 1950, 1951] was studied. Burlaga [1988] studied the above solution with constant alpha  
373 to describe the types of signatures observed in the SW at 1 AU when MCs travel through  
374 of a spacecraft. He concluded that the observed magnetic field profiles depend on the  
375 position and orientation of the axis of the MC. We written the force-free model solution

376 as Burlaga [1988]:

$$\text{Axial component : } B_A = B_0 J_0(\alpha R),$$

$$\text{Tangential component : } B_T = B_0 H J_1(\alpha R),$$

$$\text{Radial component : } B_R = 0,$$

$$\text{Total magnetic field : } B = \sqrt{B_A^2 + B_T^2 + B_R^2}, \quad (1)$$

377 where  $H = \pm 1$ , the sign providing the handedness of the field helicity, and where  $B_0$   
 378 is an estimate of field at the axis of the cloud and  $R$  is the radial distance from the  
 379 axis,  $J_0$  and  $J_1$  are the Bessel function of the first kind of order 0 and 1. The above  
 380 equations were plotted in Figure 11. The magnitude of the magnetic field at any instant  
 381 is  $B$ , which decreases from a maximum  $B_{max}$  on the axis of the MC to  $\sim 0.5B_{max}$  at the  
 382 outer boundary. Following Burlaga [1988], we show the boundaries with two vertical line  
 383 in Figure 11 as the points where  $B_A = 0$ , i.e. where  $\alpha \cdot R = 2.4$  and  $B/B_0 = 0.5$ .

384 Time series with 2001 points inside the boundaries of the cloud shown in Figure 11  
 385 are constructed. On other hand, we obtained the recurrence plots of  $B_A$ ,  $B_T$  and  $B$   
 386 respectively. After that, the STE values are calculated; with the STE of  $B_A = 27\%$ ; STE  
 387 of  $B_T = 0\%$ ; STE of  $B = 25\%$ .

388 Those low STE values are the physical justification of our results. If the spacecraft  
 389 crosses near the cloud axis then zero entropy values of some IMF components of the  
 390 structure are consequences of a nearly cylindrically symmetric force-free field. These  
 391 results reinforce our initial hypothesis that STE could be established as a feature or  
 392 tool to help in analysis of IMF data for the MC identification, mainly when the only  
 393 measurements obtained by satellites are the IMF.

## 6. Conclusions

394 In this work, using the recurrence plot (RP) technique, a methodological approach is  
395 established in order to obtain the spatio-temporal entropy (STE) related to magnetic  
396 cloud (MC) periods. The method presented in Eugene Kononov's VRA software provides  
397 resource for this kind of analysis. For this investigation, the interplanetary magnetic fields  
398 from a complete solar wind data framework are investigated.

399 The analyses developed show that the STE values for MCs are lower than the ones for  
400 sheath region or the solar wind background.

401 The reason is that in MC the magnetic field strength is higher than the average, the  
402 magnetic field direction rotates smoothly through a large angle. Then periods of MCs have  
403 more trend than sheaths region and quiet SW periods. The trend is the principal cause of  
404 the lower values of STE. It can be noticed that inside MC the IMF have less fluctuations  
405 and less noise than outside its boundary. **MCs have magnetic field more structured than**  
406 **sheath and quiet SW**. This also collaborates for the decrease of STE within the MC region.

407 Also, the differences among the STE values for the three magnetic components in a MC  
408 give an idea about the anisotropy in the structure of MCs. Those features are related to the  
409 flux-rope structure orientation, based on concepts as presented by Bothmer and Schwenn  
410 [1994, 1998]. By using a force free model for IMF as presented by Burlaga [1988], a test  
411 considering the magnetic components, mainly the tangential component, of a cylindrically  
412 symmetric force-free field constructed analytically results zero STE value. It agrees with  
413 the physical assumption of finding zero STE values when studying experimental data in  
414 MC periods.

415 The new feature just examined here adds to the usual features, as described in Burlaga  
416 et al. [1981], for the characterization of MCs. Thus, the STE calculation can be an  
417 auxiliary objective tool to identify flux-ropes associated with MCs, mainly during events  
418 with no available plasma data but only with IMF.

### Appendix A: The Recurrence Plots In Visual Recurrence Analysis Software

419 A summary of the ideas expressed in the Eugene Kononov's Visual Recurrence Analysis  
420 (VRA) software (VRA v4.7 <http://nonlinear.110mb.com/vra/>) about recurrence plots  
421 (RPs) is presented. In order to present the ideas, some figures are used to guide the  
422 description. Figure 12 (top panel) shows a recurrence plot (RP) for a simple sine wave,  
423 using the data file just included in VRA software. In it organized patterns of color  
424 characteristics are shown for the periodical signal. In order to allow a comparative view,  
425 a RP of white noise is shown in Figure 12 (bottom panel), with the data file also included.  
426 With a different result, an uniform distribution of color characteristics is noticed for the  
427 random signal.

428 The RP is a relatively recent technique for the qualitative assessment of time series [Eck-  
429 mann et al., 1987]. This technique allows someone detects hidden patterns and structural  
430 changes in data or see similarities in patterns across the time series under analysis using  
431 graphical representation. The fundamental assumption underlying the idea is that an  
432 observable time series (a sequence of observations) is the manifestation of some dynamic  
433 process.

434 It has been proved mathematically that one can recreate a topologically equivalent  
435 picture of the original multidimensional system behavior by using the time series of a  
436 single observable variable [Takens, 1981]. The basic idea is that the effect of all the

437 other (unobserved) variables is already reflected in the series of the observed output.  
 438 Furthermore, the rules that govern the behavior of the original system can be recovered  
 439 from its output.

440 In the RPs a one-dimensional time series from a data file is expanded into a higher-  
 441 dimensional space, in which the dynamic of the underlying generator takes place. This  
 442 is done by a technique called “delayed coordinate embedding”, which recreates a phase  
 443 space portrait of the dynamical system under study from a single (scalar) time series.  
 444 To expand a one-dimensional signal into an M-dimensional phase space, one substitutes  
 445 each observation in the original signal  $X(t)$  with vector  $(y(i) = \{x(i), x(i - d), x(i - 2d),$   
 446  $\dots, x(i - (m - 1)d\})$ , where  $i$  is the time index,  $m$  is the embedding dimension,  $d$  is the time  
 447 delay. As a result, we have a series of vectors  $Y = y(1), y(2), y(3), \dots, y(N - (m - 1)d)$ ,  
 448 where  $N$  is the length of the original series.

449 With such reconstruction it is possible to reproduce the original system states at  
 450 each time where we have an observation of that system output. Each unknown  
 451 state  $Z(t)$  at time  $t$  is approximated by a vector of delayed coordinates  $Y(t) =$   
 452  $x(t), x(t - d), x(t - 2d), \dots, x(t - (m - 1)d$ . After the Euclidean distances between all  
 453 vectors are calculated, they are mapped to colors from the pre-defined color map and are  
 454 displayed as colored pixels in their corresponding places (see Figure 12 (top panel), for  
 455 example). The RP is a graphical representation of a correlation integral. The important  
 456 distinction (and an advantage) is that the RP, unlike the correlation integrals, preserve  
 457 the temporal dependence in the time series, in addition to the spatial dependence.

458 In RPs, if the underlying signal is truly random and has no structure, the distribution  
 459 of colors is uniform and does not have any identifiable patterns (see Figure 12 (bottom

460 panel), for example). There is some determinism in the signal generator, which can be  
461 detected by some distinctive color distribution. For example, hot colors (yellow, red, and  
462 orange) can be associated with small distances between the vectors, while others colors  
463 (blue, black) may be used to show large distances. In this printed work colors are noticed  
464 as a grey pattern (from white to black). Therefore one can visualize and study the motion  
465 of the system trajectories and infer some characteristics of the dynamical system that  
466 generated the time series. Also, the length of diagonal line segments of the same color  
467 on the RP brings an idea about the signal predictability. But, RP is mostly a qualitative  
468 tool.

469 For random signals, the uniform (even) distribution of colors over the entire RP is  
470 expected. The more deterministic the signal, the more structured the RP. So for the  
471 purpose of comparison in Figure 12 (top panel) the RP of a strictly periodic signal can  
472 see and in Figure 12 (bottom panel) the RP of the white noise time series.

473 For force-free model solution, the recurrence plots of  $B_A$ ,  $B_T$  are shown at Figures 13,  
474 top and bottom panels respectively.

## Appendix B: The Entropy Concepts In Recurrence Plot

475 The RP is a visual tool for the investigation of temporal recurrence in phase space  
476 [Takens, 1981]. With the purpose of reaching a quantitative tool in this work, a brief  
477 review about some methods to calculate the entropy in the RP and the phase space is  
478 presented here.

479 The calculation of the spatio-temporal entropy, called in short way as STE was used  
480 to measures the image “structuredness” in a bidimensional representation, *i.e.*, both in  
481 “space” and time domains. Its implementation in VRA software is to quantify the order



482 found in RPs. The result is normalized and presented as a percentage of “maximum”  
 483 entropy (randomness). When the entropy has a value of 100% it means the absence of any  
 484 structure whatsoever (uniform distribution of colors, pure randomness, seen in Figure 12  
 485 (bottom panel)). **In particular**, 0% of entropy implies “perfect” structure (distinct color  
 486 patterns, perfect “structuredness” and predictability, seen in Figure 12 (top panel)).

487 Recurrence is the most important feature of chaotic systems [Eckmann et al., 1987].  
 488 The popularity of RPs lies in the fact that their structures are visually appealing, and  
 489 that they allow the investigation of high dimensional dynamics by means of a simple two-  
 490 dimensional plot [Facchini et al., 2009]. For a better understanding and quantification  
 491 of the recurrences, Webber and Zbilut [1994] have proposed a set of quantification mea-  
 492 sures, which are mainly based on the statistical distribution of the line structures in the  
 493 RP. Recurrence quantification analysis (RQA) is a nonlinear technique used to quantify  
 494 the information supplied by a RP [Zbilut and Webber, 1992; Webber and Zbilut, 1994].  
 495 Recurrence variables are calculated from the upper triangular area of the recurrence plot,  
 496 excluding the central diagonal, because the plot is symmetrical about the main diagonal.  
 497 The RQA can be used as a tool for the exploration of bifurcation phenomena and dynam-  
 498 ics changes also in nonstationary and short time series. The entropy (ENT) is one of the  
 499 recurrence variables of the RQA method. It is the Shannon information entropy for the  
 500 distribution probability of the diagonal lines. That is:

$$ENT = - \sum_{k=L_{min}, p(k) \neq 0}^{L_{max}} p(k) \log_2(p(k)), \quad (B1)$$

501 where  $L_{min}$  is the minimum length of diagonal lines in RP and

$$p(k) = \frac{\text{number of diagonal lines of length } k \text{ in RP}}{\text{number of diagonal lines in RP}}. \quad (B2)$$

502 The ENT can be calculated using the VRA software; but it should not be confused with  
503 the STE.

504 Little et al. [2007] developed a Recurrence Period Density Entropy (RPDE) method,  
505 first it requires the embedding of a time series in phase space, which, according to Taken's  
506 embedding theorems, can be carried out by forming time-delayed vectors for each value  
507  $x_n$  in the time series. Then, around each point in the embedded phase space, a recurrence  
508 neighbourhood of radius  $\epsilon$  is created. All recurrences into this neighbourhood are tracked,  
509 and the time interval  $T$  between recurrences is recorded in a histogram. This histogram  
510 is normalized to create an estimate of the recurrence period density function  $p(T)$ . The  
511 normalized entropy of this density is the RPDE value  $H_{norm}$  [Little et al., 2007].

$$H_{norm} = -(\ln(T_{max}))^{-1} \sum_{t=1}^{T_{max}} p(t) \ln(p(t)). \quad (B3)$$

512 The RPDE value is a scalar in the range zero to one. For purely periodic signals,  
513  $H_{norm} = 0$  (STE=0%) whereas for purely uniform white noise,  $H_{norm} = 1$  (STE=100%).  
514 However, estimates obtained with this technique (RPDE) are different from those obtained  
515 with the STE.

516 Dasan et al. [2002] report an analysis, using the tools of nonlinear dynamics and chaos  
517 theory, of the fluctuations in the stress determined from simulations of shear flow of  
518 Stokesian suspensions. They also computed the STE using VRA for the stress. The  
519 calculated values of the STE for the shear and normal stresses were nearly zero, showing  
520 perfect structure in the data. They observed definite structure in the phase-space plot of  
521 the stress components [Dasan et al., 2002]. They cited the works of Peacock [1983]; Carr  
522 and Schwartz [1998]. Peacock [1983] presented a two-dimensional analogue of Kolmogorov-

Smirnov test, useful for analysing the distribution of data in two dimensions, as is the  
 RP. Carr and Schwartz [1998] investigated the fluctuation phenomena in plasmas that  
 often needs the analysis of spatio-temporal signals. It was shown how such signals can be  
 analyzed using the biorthogonal decomposition, which splits them into orthogonal spatial  
 and temporal modes. Several parameters allow one to quantify the weight distribution in  
 the biorthogonal decomposition. The total energy of spatio-temporal signal is found to  
 be equal to the sum of the eigenvalues,  $\alpha_m$ :

$$E(u) = \sum_{m=1}^N \alpha_m^2. \quad (\text{B4})$$

They can define the relative energy of the  $m^{\text{th}}$  structure as

$$E_m(u) = \frac{\alpha_m^2}{E(u)}, \quad (\text{B5})$$

and the entropy of the spatio-temporal signal  $u(t, j)$  is defined as

$$H(u) = -\frac{1}{\log N} \sum_{m=1}^N E_m(u) \log E_m(u). \quad (\text{B6})$$

It describes how the energy is distributed across the  $N_s$  significant structures. Signal whose  
 energy is concentrated in a single structure such that  $N_s = 1$  will have very low entropy  
 $H(u) = 0$ , or  $H(u) = 1$  if the energy is distributed equally among the  $N_s$  significant  
 structures. Further, the results presented in this paper shows the usefulness of STE  
 implemented by Eugene Kononov's software to study MCs.

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**Table 1.** Summary of seven previous studies that identified MCs before 2003. In column one: 1- Bothmer and Rust [1997], 2- Bothmer and Schwenn [1998], 3- Mulligan et al. [1998], 4- Lynch et al. [2003], 5- Wu et al. [2003], 6- Huttunen et al. [2005], 7- Nieves-Chinchilla et al. [2005].

Paper	Period	$T_t$ (years)	Spacf	MC
1	1965-1993	28	OMNI	67
2	12/1974-07/1981	6.7	Helios 1/2	45
3	1979-1988	10	Pioneer	61
4	02/1998-07/2001	3.5	ACE	56
5	1995-2002	8	WIND	71
6	1997-2003	7	WIND/ACE	73
7	2000-2003	4	WIND/ACE	35

<sup>a</sup> SOURCE: Adapted from Huttunen et al. [2005].

**Table 2.** Solar Wind data studied (from Huttunen et al. [2005]).

No.	Year	Shock	UT	Start	UT	Stop	UT
01	1998	06 Jan	13:19	07 Jan	03:00	08 Jan	09:00
02		03 Feb	13:09	04 Feb	05:00	05 Feb	14:00
03		04 Mar	11:03	04 Mar	15:00	05 Mar	21:00
04		01 May	21:11	02 May	12:00	03 May	17:00
05		13 Jun	18:25	14 Jun	02:00	14 Jun	24:00
06		19 Aug	05:30	20 Aug	08:00	21 Aug	18:00
07		24 Sep	23:15	25 Sep	08:00	26 Sep	12:00
08		18 Oct	19:00	19 Oct	04:00	20 Oct	06:00
09		08 Nov	04:20	08 Nov	23:00	10 Nov	01:00
10		13 Nov	00:53	13 Nov	04:00	14 Nov	06:00
11	1999	18 Feb	02:08	18 Feb	14:00	19 Feb	11:00
12		16 Apr	10:47	16 Apr	20:00	17 Apr	18:00
13		08 Aug	17:45	09 Aug	10:00	10 Aug	14:00
14	2000	11 Feb	23:23	12 Feb	12:00	12 Feb	24:00
15		20 Feb	20:57	21 Feb	14:00	22 Feb	12:00
16		11 Jul	11:22	11 Jul	23:00	13 Jul	02:00
17		13 Jul	09:11	13 Jul	15:00	13 Jul	24:00
18		15 Jul	14:18	15 Jul	19:00	16 Jul	12:00
19		28 Jul	05:53	28 Jul	18:00	29 Jul	10:00
20		10 Aug	04:07	10 Aug	20:00	11 Aug	08:00
21		11 Aug	18:19	12 Aug	05:00	13 Aug	02:00

Continue

**Table 3.** Continuation of Table 2.

No.	Year	Shock	UT	Start	UT	Stop	UT
22		17 Sep	17:00	17 Sep	23:00	18 Sep	14:00
23		02 Oct	23:58	03 Oct	15:00	04 Oct	14:00
24		12 Oct	21:36	13 Oct	17:00	14 Oct	13:00
25		28 Oct	09:01	28 Oct	24:00	29 Oct	23:00
26		06 Nov	09:08	06 Nov	22:00	07 Nov	15:00
27	2001	19 Mar	10:12	19 Mar	22:00	21 Mar	23:00
28		27 Mar	17:02	27 Mar	22:00	28 Mar	05:00
29		11 Apr	15:18	12 Apr	10:00	13 Apr	06:00
30		21 Apr	15:06	21 Apr	23:00	22 Apr	24:00
31		28 Apr	04:31	28 Apr	24:00	29 Apr	13:00
32		27 May	14:17	28 May	11:00	29 May	06:00
33		31 Oct	12:53	31 Oct	22:00	02 Nov	04:00
34	2002	23 Mar	10:53	24 Mar	10:00	25 Mar	12:00
35		17 Apr	10:20	17 Apr	24:00	19 Apr	01:00
36		18 May	19:44	19 May	04:00	19 May	22:00
37		01 Aug	23:10	02 Aug	06:00	02 Aug	22:00
38		30 Sep	07:55	30 Sep	23:00	01 Oct	15:00
39	2003	20 Mar	04:20	20 Mar	13:00	20 Mar	22:00
40		17 Aug	13:41	18 Aug	06:00	19 Aug	11:00
41		20 Nov	07:27	20 Nov	11:00	21 Nov	01:00

END

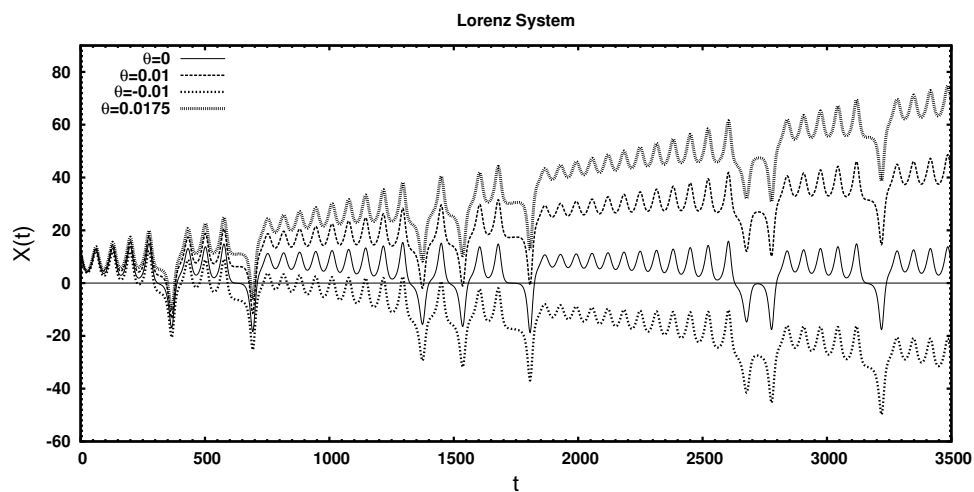
**Table 4.** STE values related to trends for three time series with data file included in VRA

4.7.

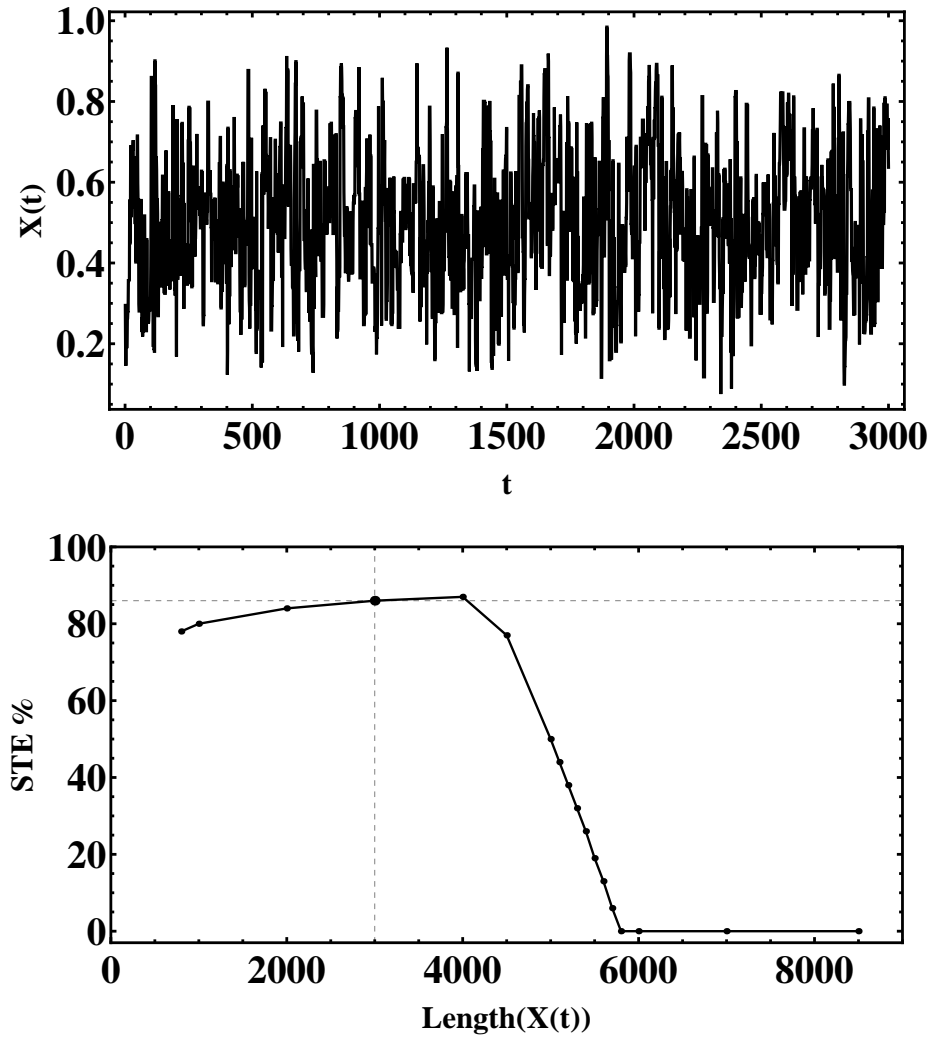
Series/angle (rad)	0	-0.01	0.01	0.0175
STE(Lorenz):	73%	30%	29%	0%
STE(Sine):	0%	0%	0%	0%
STE(White Noise):	80%	34%	34%	3%

**Table 5.** STE values related to the first-order differences in time series.

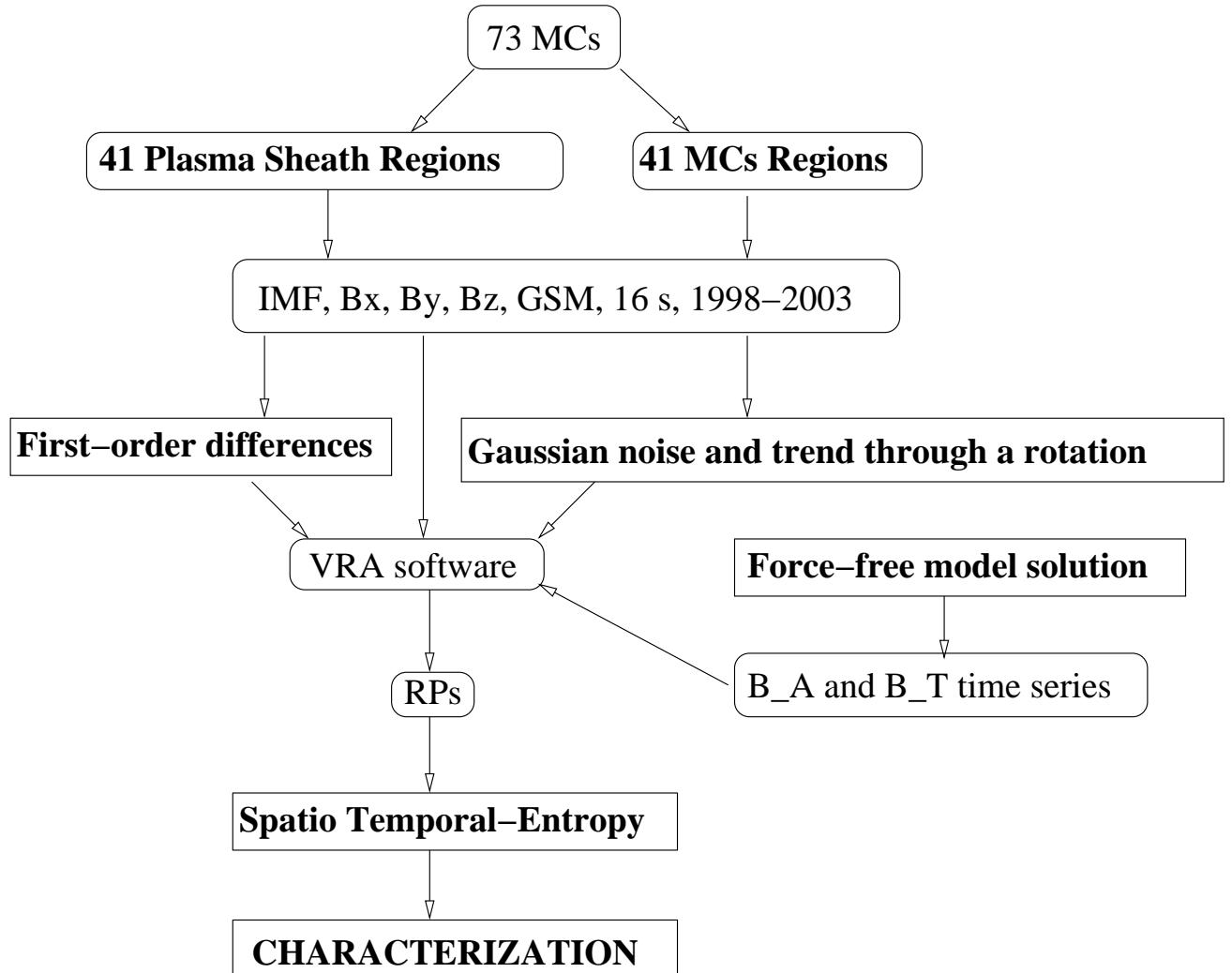
Series	Untransformed	first-order differences
STE(Lorenz)	73%	75%
STE(Sine)	0%	0%
STE(White Noise)	80%	82%



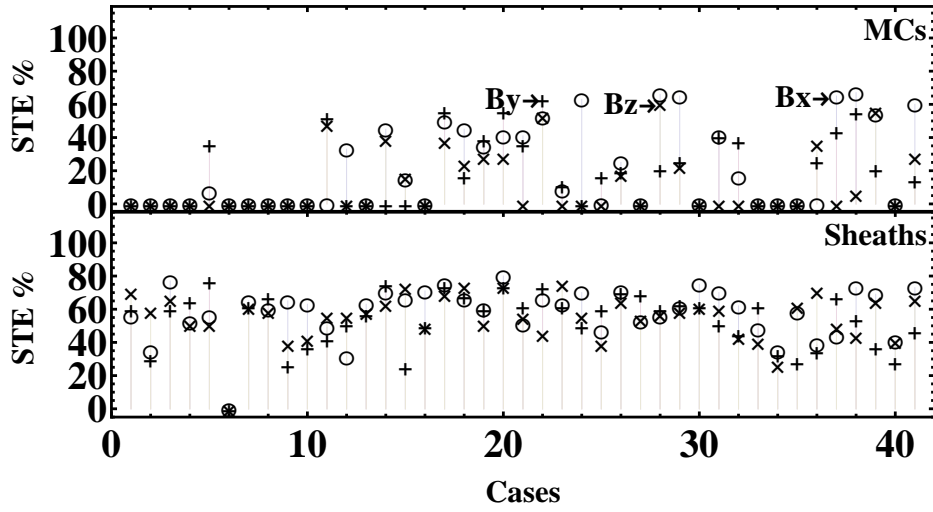
**Figure 1.** Time series plot of Lorenz data file included in VRA (case with  $\theta = 0$ ). Series rotated about origin ( $\theta = -0.01$  rad ,  $\theta = 0.01$  rad ,  $\theta = 0.0175$  rad ) and the three resulting series also plotted. After that, we calculate the STE of each time series.



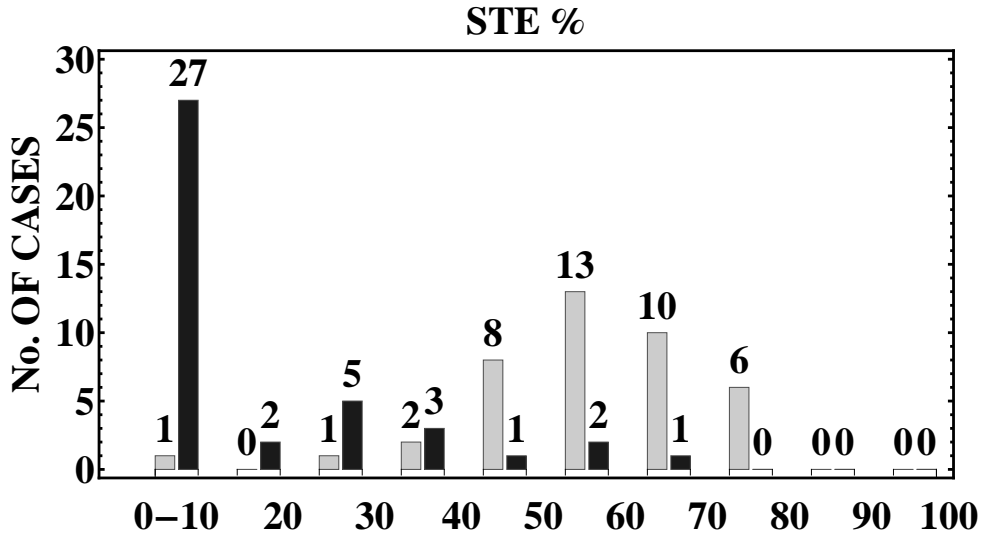
**Figure 2.** (top panel)  $X(t)$  vs  $t$  is plotted, where  $X(t)$  is a synthetic series created using a pseudorandom number generator producing values in the range 0 to 1. A simple moving average is applied to show the graph. The time series of pseudorandom number has a recurrence plot similar to shown at Figure 12 (bottom panel) and STE value of this time series is 86%. (bottom panel) The STE values versus  $\text{length}(X(t))$  of time series constructed. These values decrease in time series with a length larger than  $\sim 4000$  points.



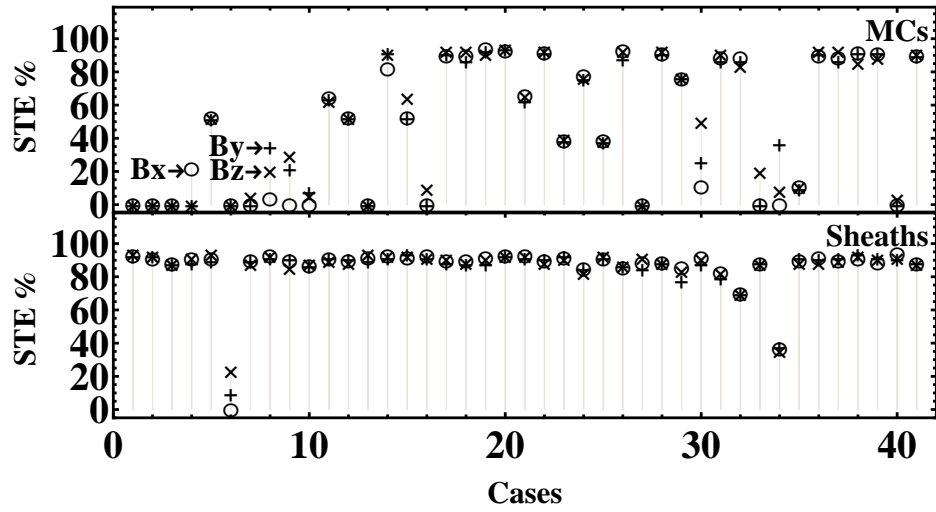
**Figure 3.** Scheme used to study 41 MCs in Section 5.



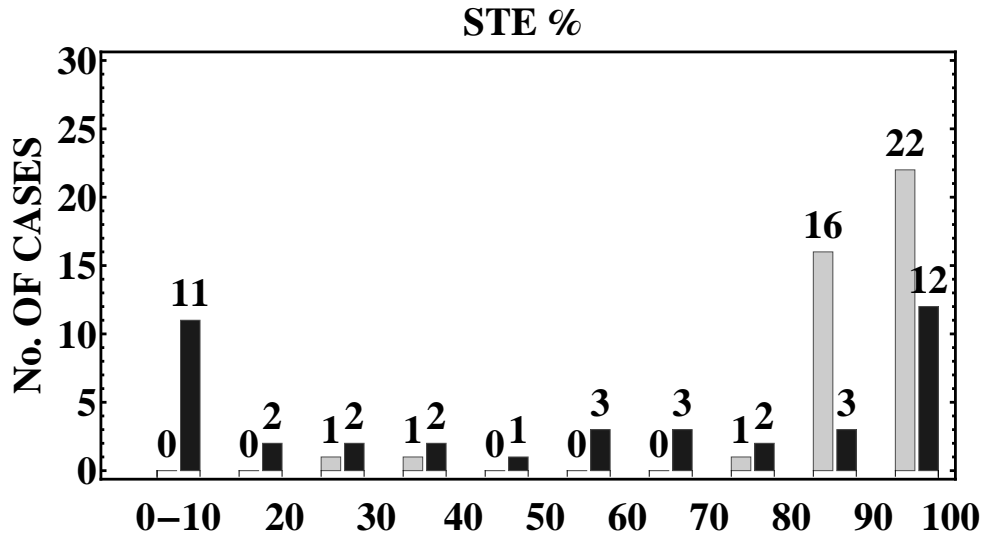
**Figure 4.** The STE values for 41 MCs from 1998 to 2003 that were presented in Table 2. At the top, the STE values for the three IMF components (“o”  $\equiv B_x$ , “+”  $\equiv B_y$ , “x”  $\equiv B_z$ ) versus cases as shown in Table 2. At bottom, the same as to above but for the sheath regions. In the two panels without previous transformation in the time series.



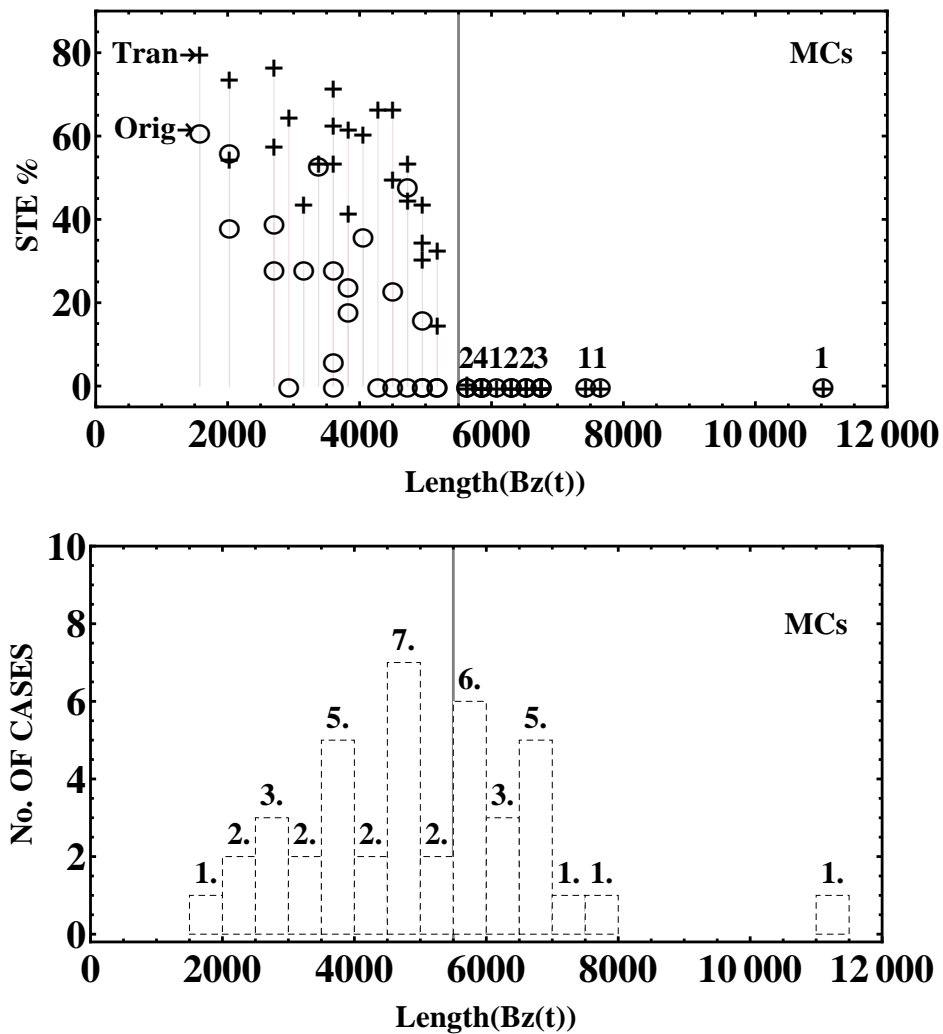
**Figure 5.** A histogram of STE derived from Figure 4 for  $B_z$  corresponding to MCs regions (in black) and plasma sheaths regions (in grey) respectively.



**Figure 6.** Format is the same as in Figure 4, but the trend was removed through the first-order differences at the time series.

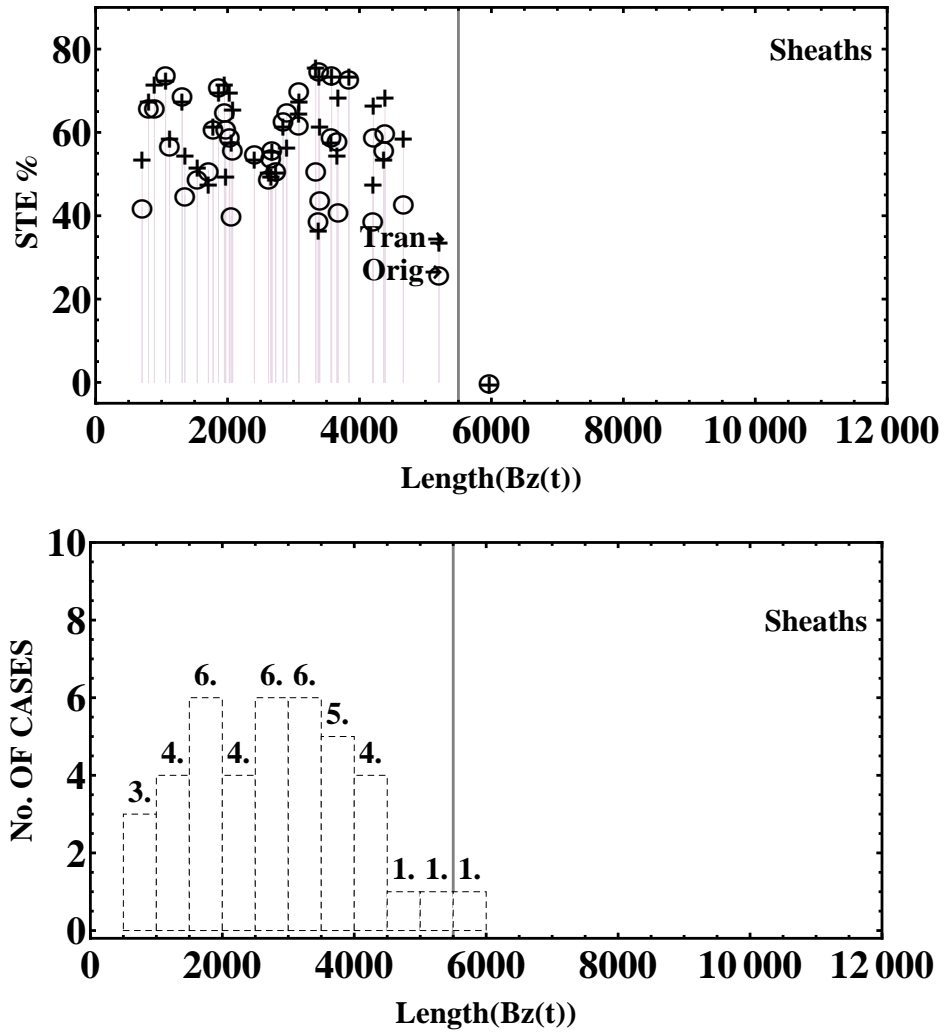


**Figure 7.** A histogram of STE derived from Figure 6 for  $B_z$  corresponding to MCs regions (in black) and plasma sheaths regions (in grey) respectively.

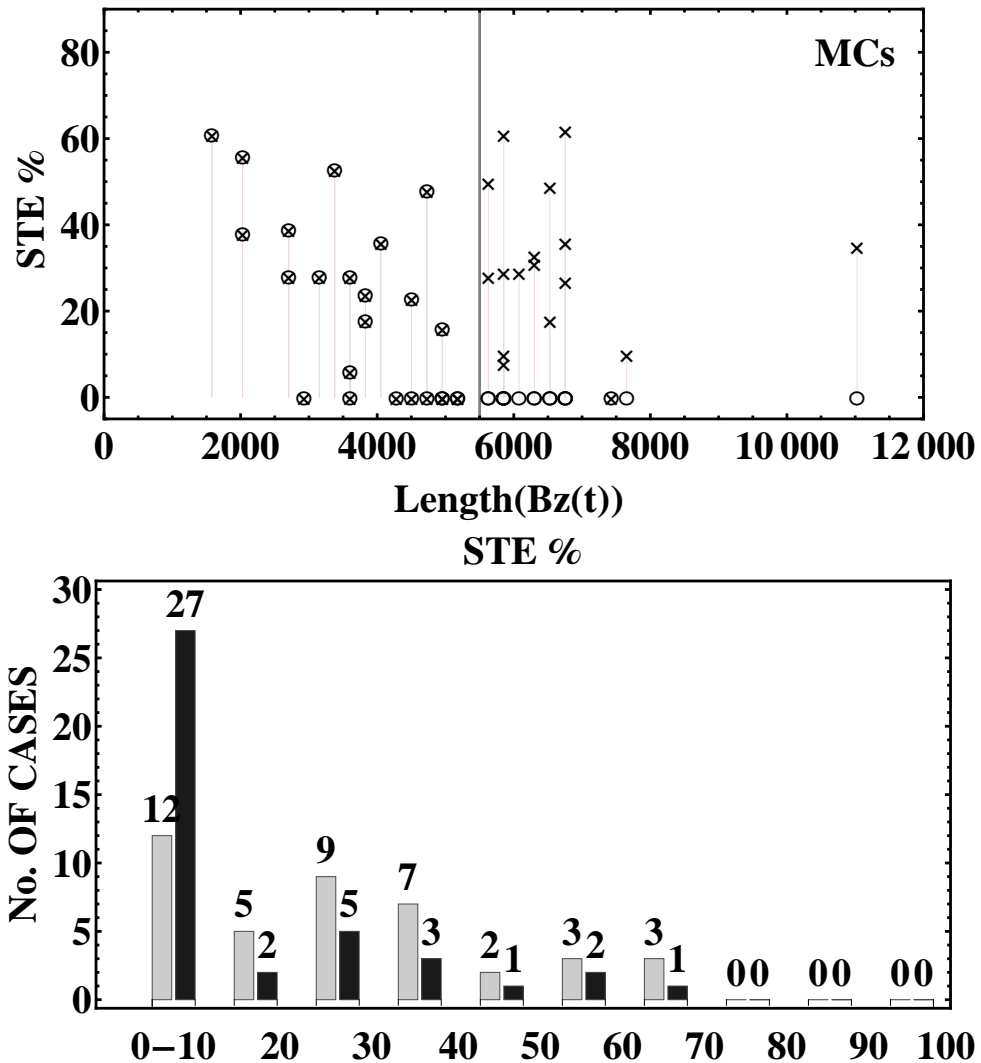


**Figure 8.** (top panel) STE values versus length of  $B_z$  time series using 41 MCs, where the “o” and “+” symbols corresponds to original and transformed (remove the Gaussian noise and trend through a rotation) time series respectively. To the right of the vertical line, larger clouds are shown, and by the software limitation the STE values are zero. (bottom panel) The histogram helps to identify overlapping points of MCs in the top panel.

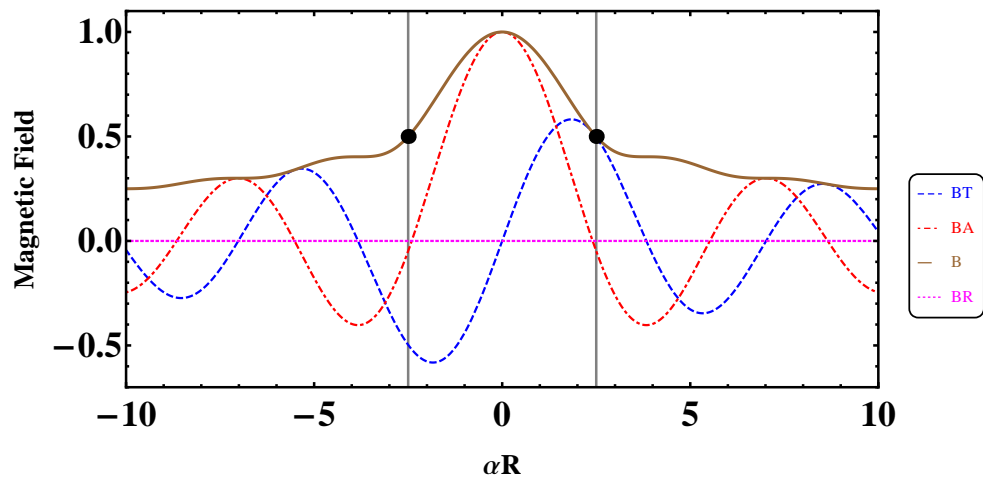




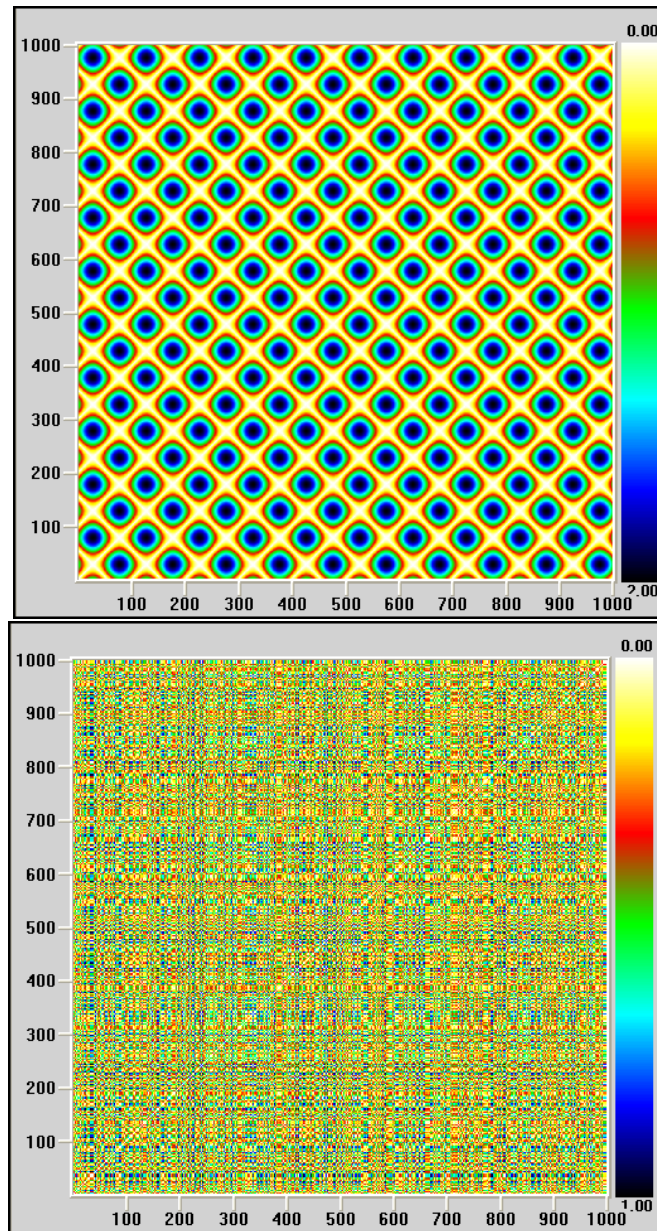
**Figure 9.** In both panels, the format is the same as in Figure 8, but STE values 41 plasma sheaths are plotted. (bottom panel) The histogram helps to identify overlapping points of sheaths in the top panel.



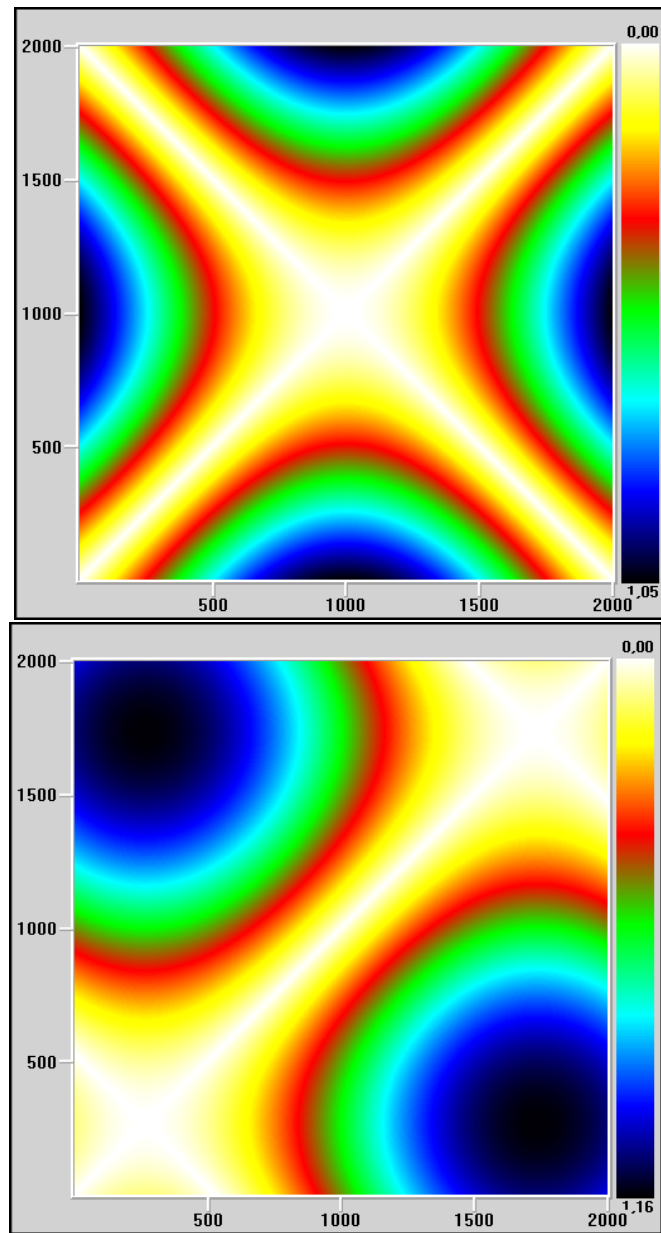
**Figure 10.** We selected MCs sample with less of 5500 points, taking the intervals between the positions 500 until 4500 in IMF  $B_z$ . (top panel) The “o” and “x” symbols correspond to non-transform and transformed (reduced to 4001 points) time series respectively. (bottom panel) A histogram of STE derived from top panel corresponding to transformed (in grey) and non-transform (in black) of  $B_z$  time series.



**Figure 11.** The force-free model solution (axial, tangential and radial components and total magnetic field) as solved in Burlaga [1988] were plotted. Following Burlaga [1988], we show the boundaries with two vertical lines at the points where  $B_A = 0$ , i.e. where  $\alpha \cdot R = 2.4$  and  $B/B_0 = 0.5$ , also  $\alpha = 1$ .



**Figure 12.** Recurrence plot using a data files included with VRA software. (top panel) In the RP organized patterns of color characteristics are shown for a periodic signal; sine wave with  $STE = 0\%$ . (bottom panel) In the RP an uniform distribution of color characteristics is shown for a random signal, white noise with  $STE = 80\%$ .



**Figure 13.** RPs of the solution for a cylindrically symmetric force-free field with constant alpha are shown. (top panel) Axial component :  $B_A = B_0 J_0(\alpha R)$ ,  $STE = 27\%$ . (bottom panel) Tangential component :  $B_T = B_0 H J_1(\alpha R)$ ,  $STE = 0\%$ .