

1 Analysis of the Breeding Technique applied to the 2 CPTEC-AGCM Model

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6 Abstract

7 The increase of understanding of the climate and weather processes
8 also supported with the evolution of the computation power has led in
9 a systematic improvement on the Numerical Weather Prediction, with
10 highly positive impact on the society activities. The NWP is becoming
11 a country-policy concern level. The models developed to simulate
12 weather behaviour became more accurate and complex, but the errors
13 in the initial conditions will be propagated during the forecasting
14 process. One approach to previous evaluation about the forecasting
15 reliability can be addressed by the breeding technique, which consist
16 in the generation and rescaling of Bred Vectors (BV).

17 Bred Vectors are the difference between reference and perturbed
18 simulations of the same model, after a time interval of integration, measured
19 with a chosen norm. The BV are periodically re-scaled to be
20 the same size of the initial perturbation for restarting the process. The
21 evolution of the BV magnitude could be used to evaluate predictability
22 and sensibility of variables.

23 The breeding technique will be applied to the Atmospheric General
24 Circulation Model (AGCM) from the CPTEC-INPE to evaluate the
25 goodness of the prediction.

26

27 **Keywords:** Bred vector, Predictability, atmospheric general circulation
28 models.

29 1 Numerical Weather Prediction

30 Numerical Weather Prediction (NWP) is a growing science with a remarkable
31 progress in the last 4 decades, where with the advent of supercomputers,
32 had led the improvement of the models generated for research and operations
33 to reach a level of huge importance for our lives.

34 Since in the beginning of last century, when Wilhelm Bjerknes [1] publish
35 a paper about the the possibility of doing weather forecast, introducing
36 concepts of hydrodynamics and thermodynamics into meteorology to solve

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37 a set of non-linear partial differential equations where the initial value prob-
38 lem can be managed by observations of the true state of the atmosphere.
39 [2]

40 Not until a few years later, Lewis Fray Richardson took this theories
41 and performed a 6 hs forecast of the evolution of the pressure, by hand and
42 after weeks of hard work he came with a totally wrong results. Later, he
43 published a book (in 1922) about his results and the difficulty to do practical
44 NWP. [2, 3].

45 Not until around the 50's that, with John Von Neumann in charge in
46 the Institute of Advance Study in Princeton, it was demonstrated that the
47 NWP was possible by producing the first 24-hours forecast using the ENIAC
48 computer. NWP gain popularity in the scientific community and by the end
49 of the decade, the forecast produced began to show steadily increasing and
50 useful skill. [2].

51 Nowadays, improvement of skills and accuracy of the different models
52 arrive as an effect of the increasing computation power which permits the
53 possibility of having high-resolutions models, accurate representations of
54 physical processes, high availability of data to represent the true state of
55 the atmosphere, etc.

56 In Brazil since 1994, The CPTEC (Centro de Previsão de Tempo e Es-
57 tudos Climáticos) has increasing its role in NWP developing a new Global
58 Atmospheric model know as BAM (Atmospheric Model) in operation since
59 January-2016. With this tool weather events such as rains, flooding and
60 others will be more accurate and help to mitigate the negative impacts in
61 the society and economy.

62 **2 Uncertanties in the model**

63 At the beginning, NWP has been used to describe the simulation of the
64 processes in the atmosphere even if this models are used for research or
65 operational purpose [4]. Today we have models that also include oceanic and
66 land processes coupled together and this interactions has a improvement in
67 the understanding and skills of the forecast.

68 The Modelling of the governing processes as a set of non-linear differen-
69 tial equation (knows as the primitive equations) consist only an approach
70 about the true state of the atmosphere where the complexity of the problem
71 is far from be a closed problem.

72 The chaotic behaviour, proved by Lorenz [5], of the atmospheric dynam-
73 ics shows a sensitivity with the initial conditions, and, as the true state of

74 the atmosphere is never known for sure (due errors in the measure instru-
 75 mentation, calibrations, others) this help in the increment of the complexity
 76 of the model and limits the predictability ² of the weather in a period of
 77 approximately two weeks at most.

78 Dealing with a such a complex model where the initial condition is sub-
 79 ject to errors, the models equations aren't known completely and it has a
 80 chaotic behaviour, has all the kind of unavoidable uncertainty sources that
 81 we can mention. As described in [3], "even if the model is perfect and even
 82 if the initial condition are almost known perfectly, like any dynamic system
 83 with instabilities still has a finite limit of predictability".

84 Another focus of uncertainties are the numerical round-off, the different
 85 numerical schemes and even the compiler used that represent the numbers
 86 in machine code have an impact in this type of systems.

87 **3 Atmospheric Global Circulation Model - AGCM**

88 Kalnay in [3] categorized the models in two categories, regional and global
 89 models. Regional Models are used for short-range forecast (typically 1-3
 90 days) with high resolution discretization, even two or more times higher
 91 than Global models, which are used generally for guidance in medium-range
 92 forecast (more than 2 days) and for climate simulations.

93 The CPTEC has both models, the regional BRAMS (Brazilian Regional
 94 Atmospheric Modeling System) and the AGCM-CPTEC Global model. This
 95 work use the AGCM model, which has a T126 horizontal configuration of
 96 spectral discretization with triangular truncation (approx 105 km of space
 97 step) and a 28 vertical layer with a time step of 1200 seconds.

98 The Global AGCM-CPTEC model operates with a higher spectral res-
 99 olutions but it was chosen T126 because it has to be in agreement with the
 100 Ensemble model used to contrast the results of the breeding technique (see
 101 section 5)

102 The principal processes including in the AGCM-CPTEC model are hy-
 103 drodynamic processes (movement equations, horizontal diffusions, etc.), su-
 104 perfacial physics of the ocean and land, vertical diffusions, deep convection
 105 and the initial (spectral analysis, initialization) and boundary conditions.
 106 [6].

²The term predictability, as defined in [4], consist in the time required for solutions from two models that are initialized with slightly different initial conditions to diverge to the point where the objective (e.g. RMS) difference is the same as that between two randomly chosen observed states of the atmosphere.

107 The prognostic variables of the AGCM-CPTEC model are: the Surface
 108 pressure logarithm, the vorticity, the divergence of the horizontal wind, the
 109 virtual temperature and the specific humidity also with the topography. The
 110 models has three interconnected parts:

- 111 • Pre-processing, dealing with the initial set-up of the variables for the
 112 model
- 113 • The model, the core of the system which has the numerical equations
- 114 • Pos-processing, necessary to perform the transform of the model out-
 115 put in spectral coordinates to a geographic coordinates for visualizing
 116 the results.

117 4 Ensemble Prediction Model

118 The Ensemble prediction model is a technique used for overcome the sources
 119 of error or uncertainties mentioned in 2, by sampling the error space asso-
 120 ciated and performing several simulations of the model with different initial
 121 conditions values.

122 Each simulation with a particular initial condition is known as a member
 123 of the ensemble and in the overall, the ensemble method is most useful that
 124 an individual, deterministic forecast [4]

125 Using statistics, i.e. mean, spread and variance, the accuracy is improved
 126 and the the difference in the members is an indication of the quantitative
 127 uncertainty of the forecast.

For example the Mean of a X-variable (Temperature, Moisture, Wind,
 etc.):

$$\bar{X} = \frac{\sum_{i=1}^n X_i}{n},$$

and spread (Standard Desviation) of X:

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n - 1}}$$

128 In the CPTEC, The forecast for ensemble method is operative since
 129 2001, with a EOF (Empiric Orthogonal Function) as a method to develop the
 130 several initial conditions. The Ensemble Model operates in a T126 resolution
 131 with 28 vertical layer and 15 (fifteen) members, where the perturbations are
 132 added (7 members) and subtracted (7 members) consistently to the control
 133 initial condition.

134 The operation of the Ensemble forecast starts for every day at 00 UTC
 135 and at 12 UTC and perform a forecasting for 15 days in advance. Figure
 136 1 shows the variability of the Ensemble Surface Temperature Global Mean
 137 and its spreads (the standard deviation) starting in 02 of December of 2014
 138 at 00 UTC and integrating to 17 of December of 2014 at 00 UTC. It worth
 139 to mention about the variability of the mean and the growing spread as a
 140 synonymous of a decay in the reliability of the forecast.

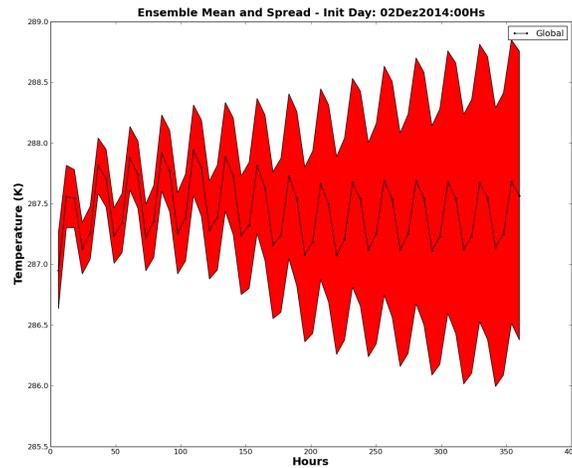


Figure 1: Ensemble Forecast of the AGCM-CPTEC model. The Ensemble Global Surface Temperature mean in black and surrounded by the spread of the 15 members in red. Simulation performed for 15 days (360 Hours)

141 Another view of the evolution of the Global Temperature Spread in the
 142 Ensemble Prediction is shown in Figure 2. As can be noticed, the spread of
 143 the Ensemble grows in the north hemisphere and in the region of Australia
 144 with a high amplitude, also but with a lower amplitude in the south-America
 145 tropical region. This growing amplitude of the spread can be associated with
 146 the lost of reliability of the prediction in those areas

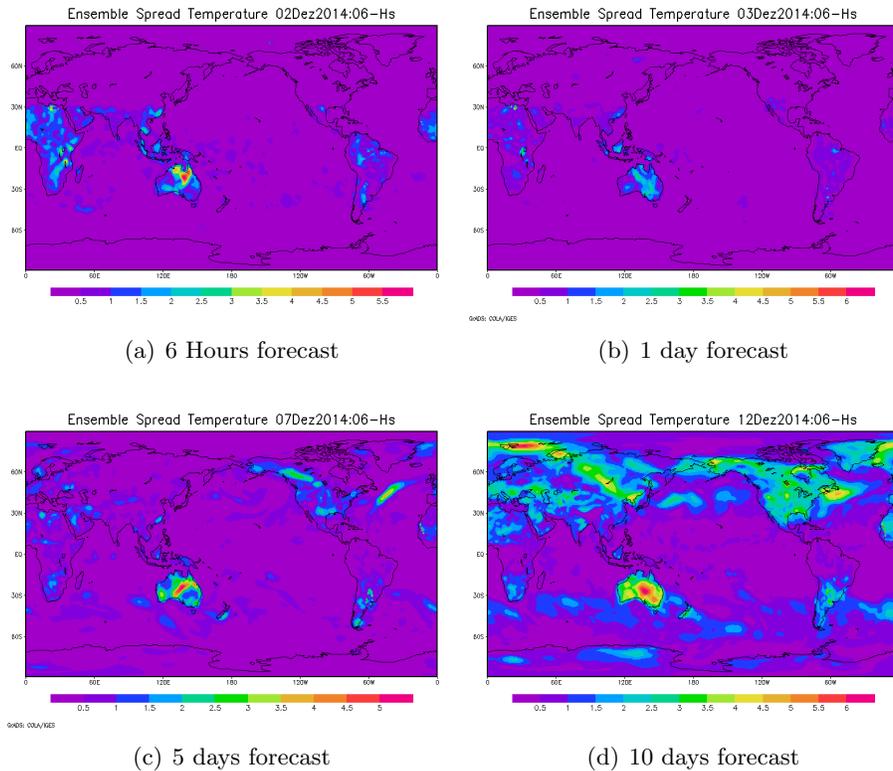


Figure 2: Global Spread of the Temperature. Source:

147 5 The Breeding Method

148 Breeding method has been used since 1992 to generate perturbation for
 149 ensemble forecasting at the NCEP, where the method simulates the devel-
 150 opment of growing errors in the analysis cycle [7]. This method, developed
 151 by Toth and Kalnay, has an important property that all random perturba-
 152 tion assume the structure of the Leading Local Lyapunov Vectors (LLLV)
 153 after a transient period (approx. 3 days).

154 This growing errors, associated with the evolving state of the atmo-
 155 sphere, dominate the subsequent forecast errors growth [7].

156 The Breeding technique consist in the integration of the same non-linear
 157 model twice, beginning with different initial conditions. The steps, described
 158 in [7], are the following (see fig. 3):

- 159 1. Add a small, arbitrary perturbation to the analysis initial state.

- 160 2. Integrate both model (control and perturbed) with its initial condi-
 161 tions for a short period ΔT (time step, normally 6 hours)
- 162 3. Subtract one forecast from the other. This difference in variable state
 163 is called Bred Vectors.
- 164 4. Scale down the difference so that it has the same size (choose a norm,
 165 e.g. rms amplitude) as the initial perturbation.
- 166 5. The perturbation resized is added to the analysis corresponding for
 167 the following time step and repeat the cycle forward in time.

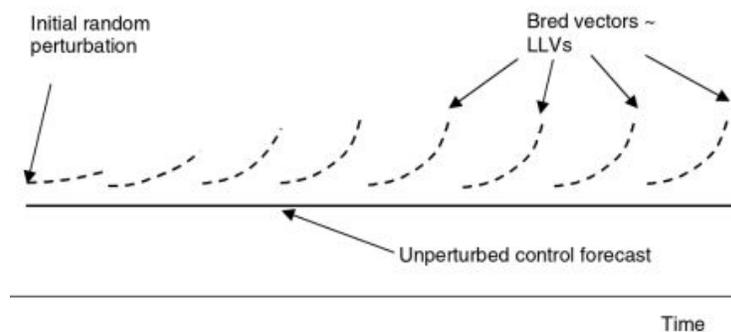


Figure 3: Schematic of the Breeding Method. Source:[3]

168 Since the construction of the Bred Vectors are related to the Lyapunov
 169 Vectors, the perturbation in space and time are similars after the transient
 170 period. This property is used to compare with the errors showed in figure 2
 171 by the ensemble forecast.

172 6 Experiments and results

173 It was performed a simulation of the breeding technique with an initial
 174 uniform perturbation in the Virtual Temperature Analysis increased by 0.1%
 175 in all the globe. The Initial date was the 02 of December of 2014 at 00 UTC.

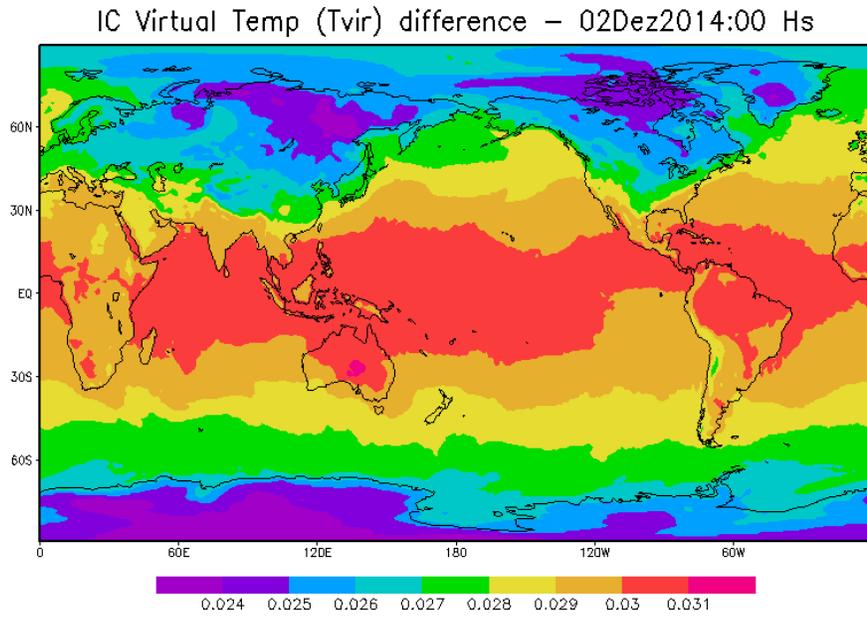


Figure 4: Initial Condition (I.C.) difference of control and perturbed model in the Virtual Temperature Analysis at the surface. Source:

The chosen norm was the rms of the difference of temperature at the entire grid:

$$Norm = \frac{\sum_{i=1, j=1}^{i=nlat, j=nlon} [Temp - Ctrl_{i,j} - Temp - Pert_{i,j}]^2}{nlat * nlon},$$

176 where $nlat$, $nlon$ are the total discretization points of latitude and longitude
 177 coordinates. The size of the initial perturbation was 0.0288016.

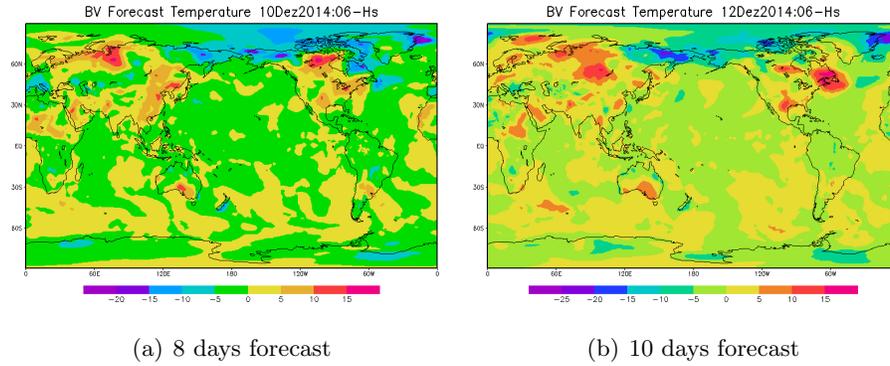
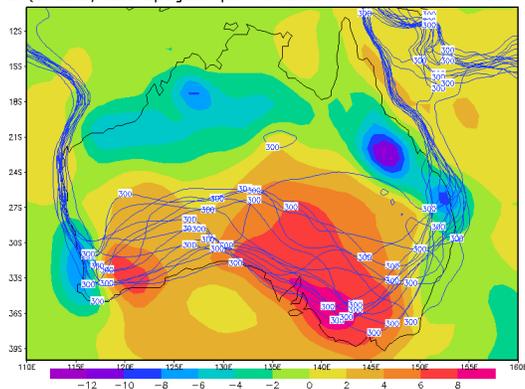


Figure 5: Bred Vectors of the Surface Temperature. Bred Vectors are the difference of the Temperature Forecast of both models, perturbed and unperturbed Source:

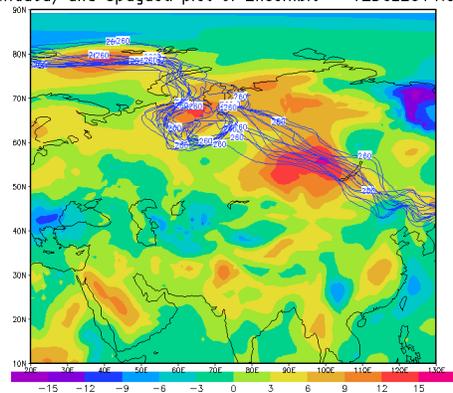
178 According with Figure 2, the regions of major spread are in Australia,
 179 North of Europe and North of America which is also in agreement with the
 180 size of major Bred Vectors showed by Figure 5.

BV(shaded) and Spagueti plot of Ensemble – 12Dez2014:06–Hs



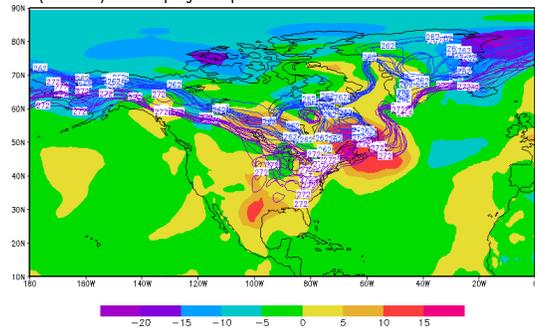
(a) Region of Australia

BV(shaded) and Spagueti plot of Ensemble – 12Dez2014:06–Hs



(b) Region of North-Europe

BV(shaded) and Spagueti plot of Ensemble – 12Dez2014:06–Hs



(c) Region of North-America

Figure 6: Bred Vectors of the Surface Temperature and spaghetti plot of the members of the Ensemble Forecasting.

181 In Figure 6 are shown the results of Bred Vectors of the surface Tem-
182 perature in shaded and some levels of temperature in spaghetti plot of the
183 ensemble members for different regions of the globe. With the spaghetti
184 plot can be see the spread of the different members of the ensemble and can
185 be inferred that in regions of great spread there is a great amplitude of the
186 Bred Vector as well, so, Bred Vectors can be used as a tool to measured de
187 reliability as well as the spread of the ensemble forecasting.

188 7 Conclusion

189 The breeding technique was applied to the AGCM-CPTEC model generating
190 Bred Vectors that indicate regions with high and low predictability. BV
191 showed that are in good agreement with the spread of the ensemble members
192 and can be used as an estimation of the reliability of the forecast taking in
193 account its simplicity and less cost of generation.

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